NAG Toolbox for MATLAB

f08ge

1 Purpose

f08ge reduces a real symmetric matrix to tridiagonal form, using packed storage.

2 Syntax

```
[ap, d, e, tau, info] = f08ge(uplo, n, ap)
```

3 Description

f08ge reduces a real symmetric matrix A, held in packed storage, to symmetric tridiagonal form T by an orthogonal similarity transformation: $A = QTQ^{T}$.

The matrix Q is not formed explicitly but is represented as a product of n-1 elementary reflectors (see the F08 Chapter Introduction for details). Functions are provided to work with Q in this representation (see Section 8).

4 References

Golub G H and Van Loan C F 1996 Matrix Computations (3rd Edition) Johns Hopkins University Press, Baltimore

5 Parameters

5.1 Compulsory Input Parameters

1: **uplo – string**

Indicates whether the upper or lower triangular part of A is stored.

```
uplo = 'U
```

The upper triangular part of A is stored.

uplo = 'L'

The lower triangular part of A is stored.

Constraint: uplo = 'U' or 'L'.

2: n - int32 scalar

n, the order of the matrix A.

Constraint: $\mathbf{n} \geq 0$.

3: ap(*) – double array

Note: the dimension of the array **ap** must be at least $\max(1, \mathbf{n} \times (\mathbf{n} + 1)/2)$.

The n by n symmetric matrix A, packed by columns.

More precisely,

if **uplo** = 'U', the upper triangle of A must be stored with element A_{ij} in $\mathbf{ap}(i+j(j-1)/2)$ for $i \le j$;

if **uplo** = 'L', the lower triangle of A must be stored with element A_{ij} in $\mathbf{ap}(i+(2n-j)(j-1)/2)$ for $i \ge j$.

[NP3663/21] f08ge.1

f08ge NAG Toolbox Manual

5.2 Optional Input Parameters

None.

5.3 Input Parameters Omitted from the MATLAB Interface

None.

5.4 Output Parameters

1: ap(*) – double array

Note: the dimension of the array **ap** must be at least $\max(1, \mathbf{n} \times (\mathbf{n} + 1)/2)$. **ap** contains the tridiagonal matrix T and details of the orthogonal matrix Q.

2: d(*) – double array

Note: the dimension of the array **d** must be at least $max(1, \mathbf{n})$.

The diagonal elements of the tridiagonal matrix T.

3: e(*) – double array

Note: the dimension of the array **e** must be at least $max(1, \mathbf{n} - 1)$.

The off-diagonal elements of the tridiagonal matrix T.

4: tau(*) – double array

Note: the dimension of the array tau must be at least max(1, n - 1).

Further details of the orthogonal matrix Q.

5: info - int32 scalar

info = 0 unless the function detects an error (see Section 6).

6 Error Indicators and Warnings

Errors or warnings detected by the function:

info = -i

If info = -i, parameter i had an illegal value on entry. The parameters are numbered as follows:

1: uplo, 2: n, 3: ap, 4: d, 5: e, 6: tau, 7: info.

7 Accuracy

The computed tridiagonal matrix T is exactly similar to a nearby matrix (A + E), where

$$||E||_2 \le c(n)\epsilon ||A||_2,$$

c(n) is a modestly increasing function of n, and ϵ is the *machine precision*.

The elements of T themselves may be sensitive to small perturbations in A or to rounding errors in the computation, but this does not affect the stability of the eigenvalues and eigenvectors.

8 Further Comments

The total number of floating-point operations is approximately $\frac{4}{3}n^3$.

To form the orthogonal matrix Q f08ge may be followed by a call to f08gf:

$$[q, info] = f08gf(uplo, n, ap, tau);$$

f08ge.2 [NP3663/21]

To apply Q to an n by p real matrix C f08ge may be followed by a call to f08gg. For example, [ap, c, info] = f08gg('Left', uplo, 'No Transpose', ap, tau, c); forms the matrix product QC.

The complex analogue of this function is f08gs.

9 Example

```
uplo = 'L';
n = int32(4);
ap = [2.07;
     3.87;
     4.2;
     -1.15;
     -0.21;
     1.87;
     0.63;
     1.15;
     2.06;
     -1.81];
[apOut, d, e, tau, info] = f08ge(uplo, n, ap)
apOut =
    2.0700
   -5.8258
    0.4332
   -0.1186
    1.4741
    2.6240
    0.8063
   -0.6492
    0.9163
   -1.6949
    2.0700
    1.4741
   -0.6492
   -1.6949
e =
   -5.8258
    2.6240
    0.9163
tau =
    1.6643
    1.2120
         0
info =
           0
```

[NP3663/21] f08ge.3 (last)